

General-purpose Multi-Phase Dynamics Program

MUFFIN

- MULTIFARIOUs FIELD simulator for NON-equilibrium system -

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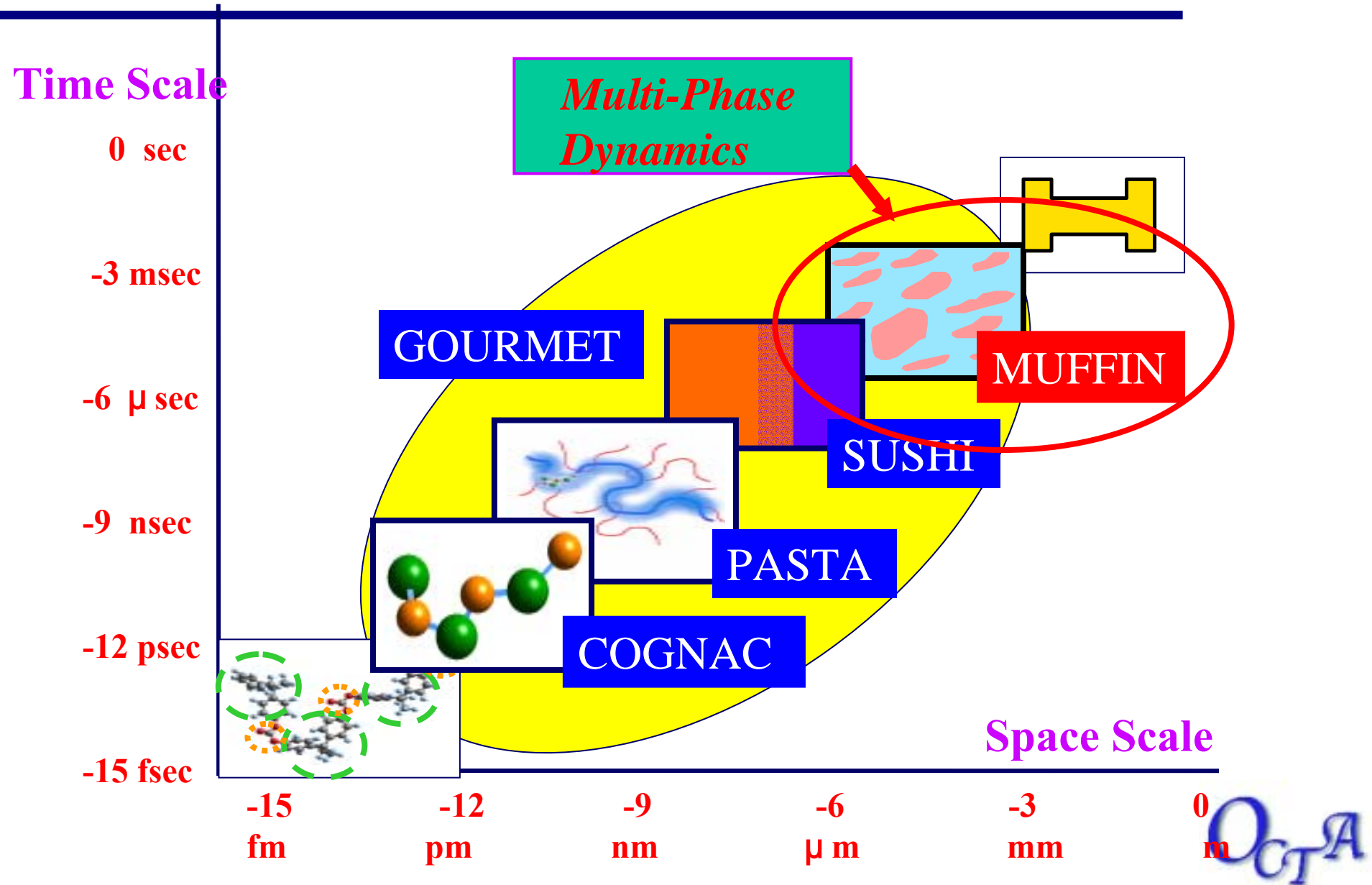
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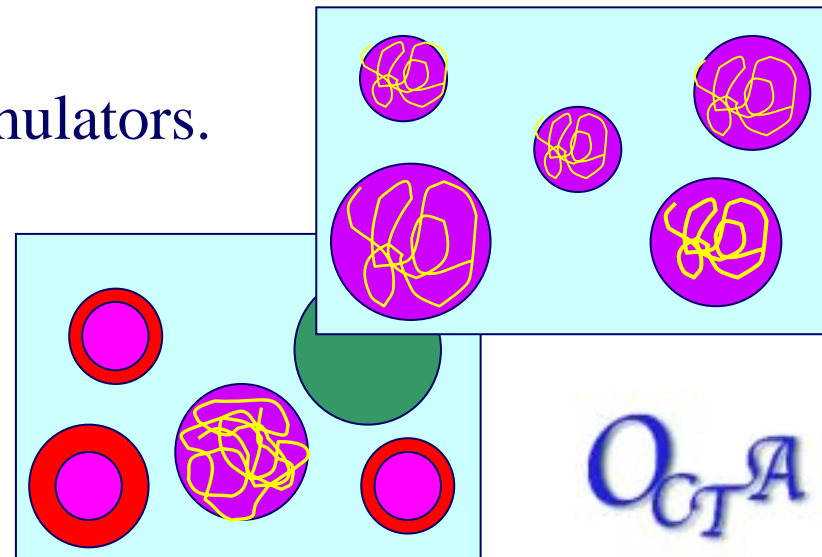
Time/Space Scales of MUFFIN



Scope of Problems handled by MUFFIN

Aim: Design and Control of Multi-Phase Structure of Polymeric Materials

- ◆ Dispersion structures.
 - Coagulation and breakup of droplets.
 - Effect of surface modification.
- ◆ Micro process control by pressure, shear, electric field, etc.
 - Micro fabrication of thin films
- ◆ Relation between stiffness and toughness, and morphology.
 - Deformation of elastic materials.
- ◆ Collaboration (zooming) with meso-simulators.
- ◆ Electrolyte fluid kinetics near electrodes.
- ◆ Chemical reaction in narrow channels.
- ◆ Swelling and deswelling of gels.



Features of MUFFIN

Various Continuum models

Various methods.

- **Finite difference method (FDM)** : Eulerian picture.
- **Finite element method (FEM)** : Eulerian and Lagrangian picture.

Various Meshes.

- **Structured mesh.**
- **Unstructured mesh (2D/3D).** (Delaunay triangulation 2D/3D)

Various Dynamics.

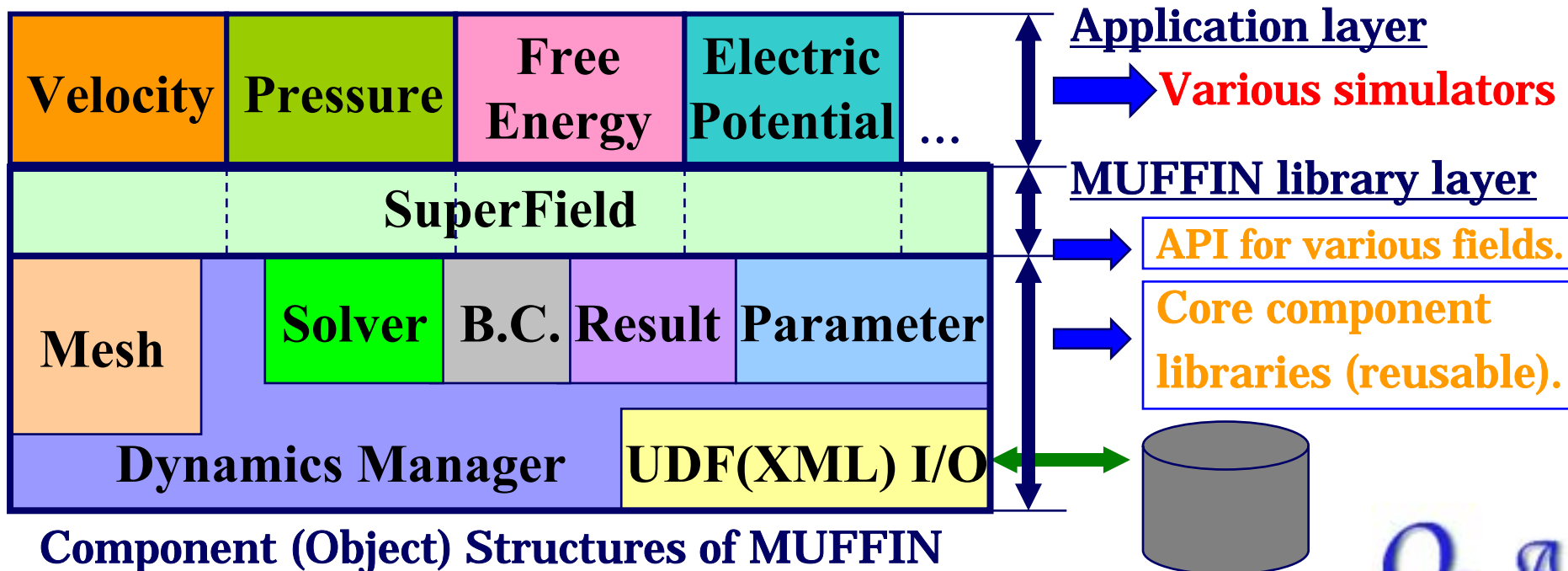
- **Free energy** : Flory-Huggins, Electro-Chemical, Elastic, Gels,....
- **Velocity** : Navier-Stokes, Stokes, Oseen, Two fluid model,.....
- **Concentration** : Diffusion and flow of polymer, solvent, counter ions,....
- **Electric potential** : Poisson, Poisson-Boltzmann,
- **Pressure**.....
- **Polymer Stress**.....
-

Architecture of MUFFIN

Object-oriented designing

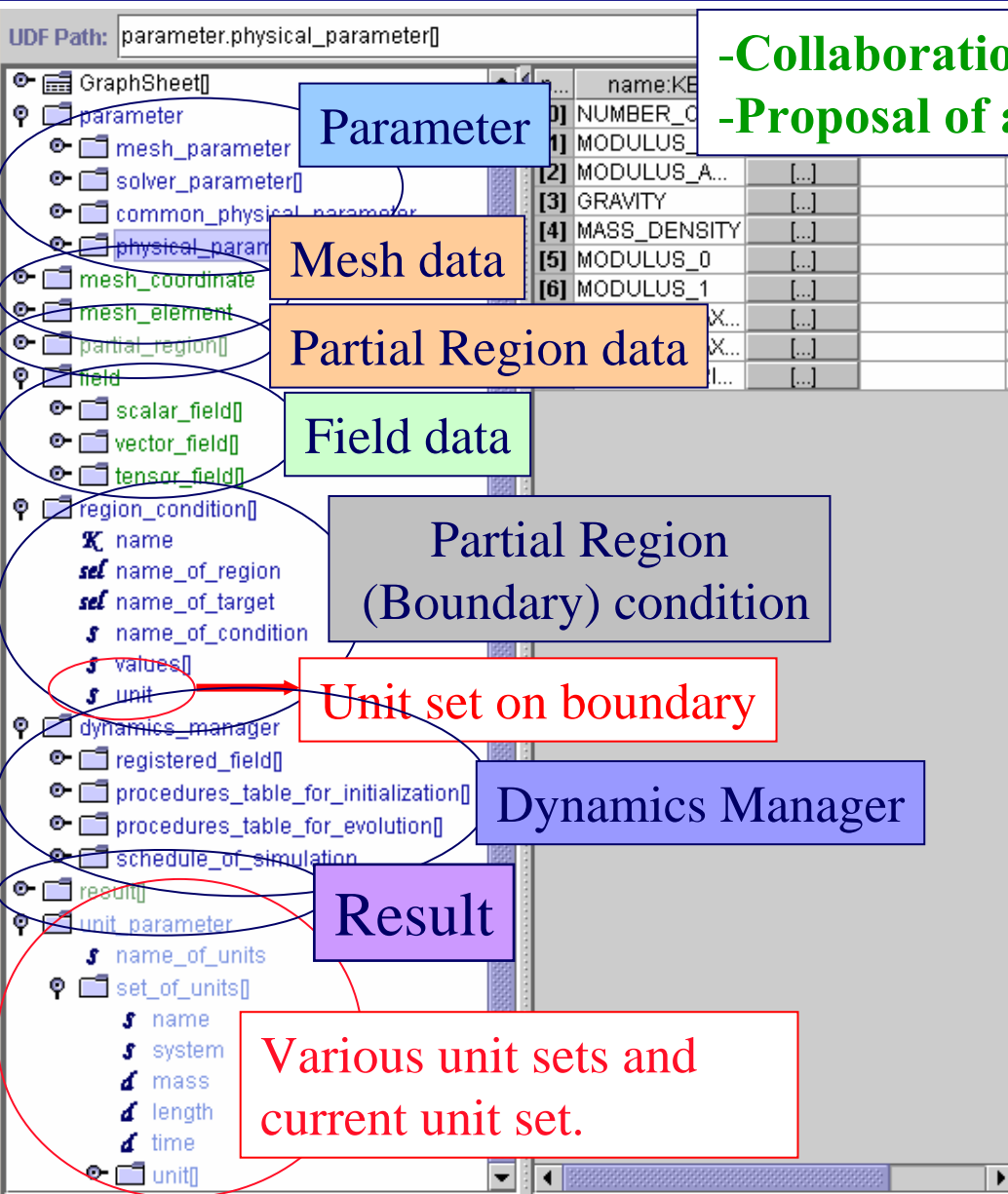
for general multi-scale continuum fields simulation

- ◆ SuperField. (base object of physical fields)
 - Equip various methods for physical fields. Message passing between different fields.
- ◆ DynamicsManager.
 - Control I/O, construct dynamics and execute simulation for given schedule.



- "MUFFIN" isn't a name of simulator but a name of architecture. -

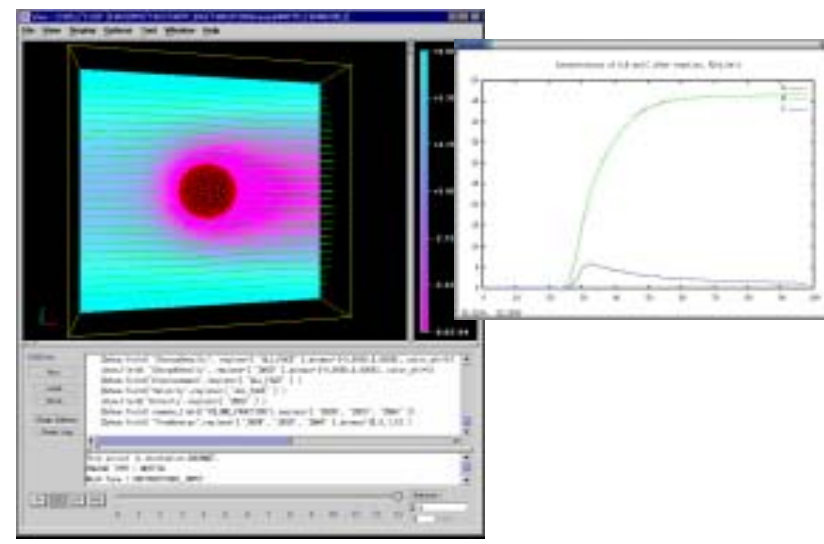
Structure of I/O data sheets of MUFFIN



-Collaboration of different simulators.
-Proposal of a Front-end of multi-scale simulator.

Visualization

Plot



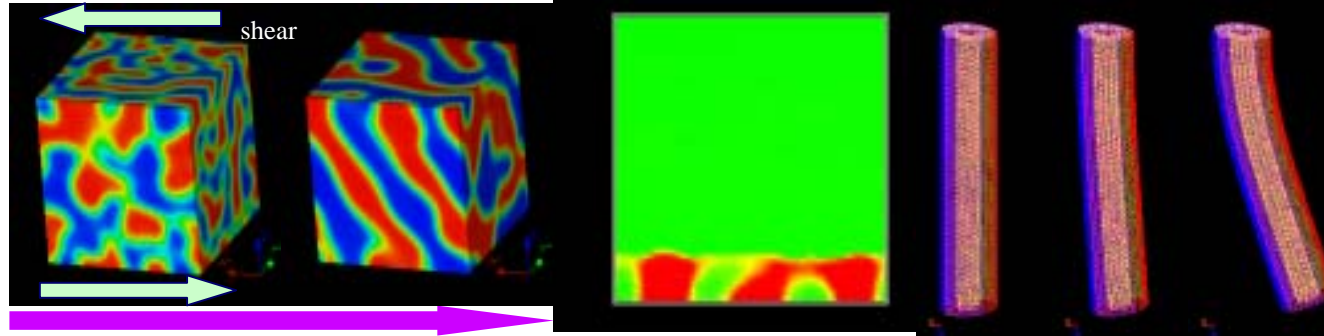
cf) XSIL (XML Scientific Interchange)
Prof. R.Williams, CACR, Caltech.
(Center for Advanced Computing Research)



Simulation Packages of MUFFIN

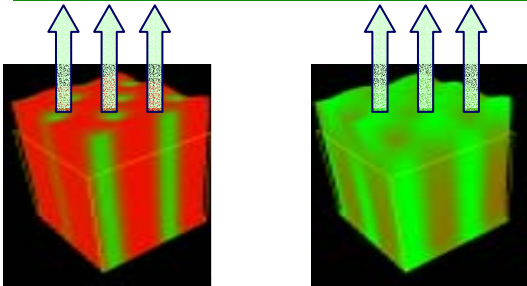
Six simulation engines (three fluid simulators, two solid simulators and one optics simulator) are now on release.

- ◆ PhaseSeparation
- ◆ Electrolyte
- ◆ MEMFluid
- ◆ Elastica
- ◆ GelDyna
- ◆ TURBAN

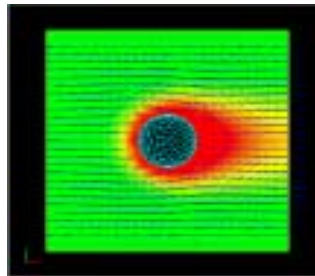


PhaseSeparation : The multi-phase dynamics simulator for polymeric fluids under the shear flow and the electric field with the hydrodynamic effect. (Fig. the phase separation dynamics of polymer blend under the shear (left), Spin coating simulation with evaporation under shear (right))

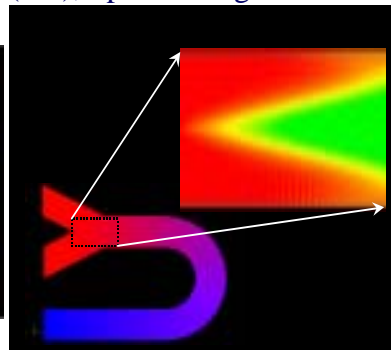
GelDyna : The large deformation dynamics simulator for multi-phase gel system by change of external stimuli, such as temperature, pH, and electric field, and external forces.



Elastica : The linear elasticity simulator for multi-phase solid system, including both isotropic and anisotropic elasticity. (Fig. the deformation (left) and strain-energy (right) of cylinder phase structure obtained by SUSHI under the external force.)



Electrolyte : The multi-component electrolyte fluid dynamics simulator under the shear flow and the electric field.



MEMFluid : The chemical reaction and extraction dynamics simulator for multi-component electrolyte fluids in the micro-fluidity chip.

TURBAN : The light transmittance simulator



“Phase Separation”

The equations of Phase Separation

Basic model:

$$\frac{\partial \psi^\alpha}{\partial t} = -\nabla \cdot (\psi^\alpha \mathbf{v}) + \nabla \cdot (L_\alpha \nabla \mu_\alpha)$$

$$\rho \frac{\partial \mathbf{v}}{\partial t} = -\nabla p + \nabla \left[\eta \left\{ \nabla \mathbf{v} + (\nabla \mathbf{v})^t \right\} \right] + \mathbf{K}$$

$$\nabla \cdot \mathbf{v} = 0$$

Flow: incompressible, slow flow (Stokes flow $\nu / t = 0$)

Chemical potential μ , driving force \mathbf{K} are derived from the functional of the free energy. L is the transport coefficient.

Examples of the free energy functional

Flory-Huggins

$$F^{(FH)} = \frac{k_B T}{v_o} \int dV \left[\sum_{\alpha=0}^{M-1} \frac{\psi_\alpha}{N_\alpha} \ln \psi_\alpha + \sum_{\alpha < \alpha'}^{M-1} \chi_{\alpha\alpha'} \psi_\alpha \psi_{\alpha'} + \frac{1}{2} \sum_{\alpha < \alpha'}^{M-1} C_{\alpha\alpha'}(\psi_\alpha, \psi_{\alpha'}) [\nabla(\psi_\alpha - \psi_{\alpha'})]^2 \right]$$

Multi component fluid under an electric field

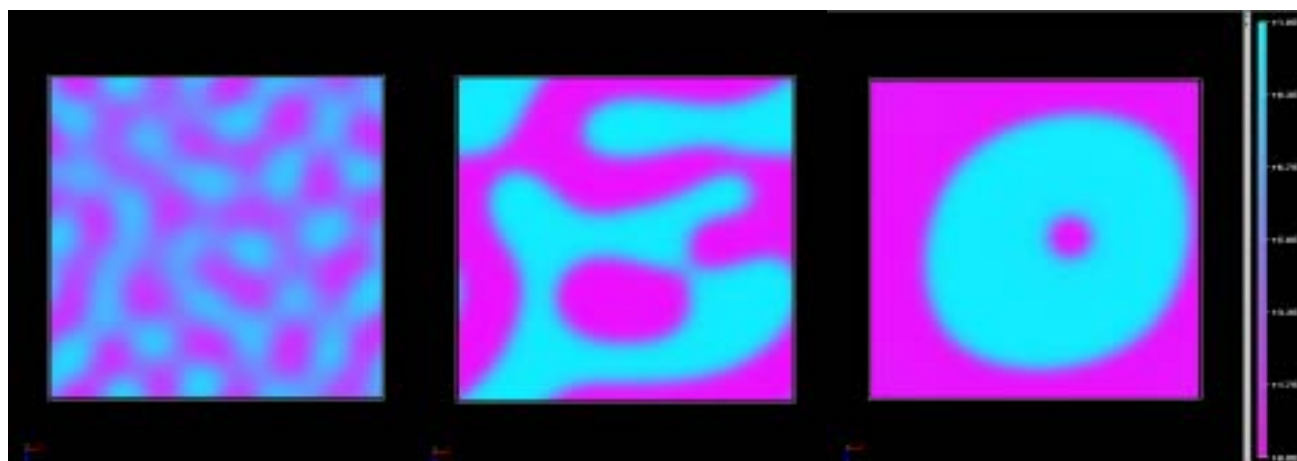
$$F = F_{mix} + \int dV \left[-\frac{1}{2} \epsilon(\{\psi_\alpha\}, T) \mathbf{E}^2 + \frac{1}{2} \rho_\epsilon(\{\psi_\alpha\}) \Phi \right]$$

$$\mu_\alpha^{(X)} = \mu_{\alpha mix}^{(X)} - \frac{1}{2} (\epsilon_\alpha - \epsilon_0) \mathbf{E}^2 + (\rho_{\epsilon\alpha} - \rho_{\epsilon 0}) \Phi$$

$$\mathbf{K} = - \sum_{\alpha=1}^{M-1} \psi_\alpha \nabla \mu_\alpha$$

$$\nabla \cdot \left[\epsilon(\mathbf{r}) \nabla \Phi \right] = -\rho_\epsilon(\mathbf{r})$$

Applications of “PhaseSeparation FDM”



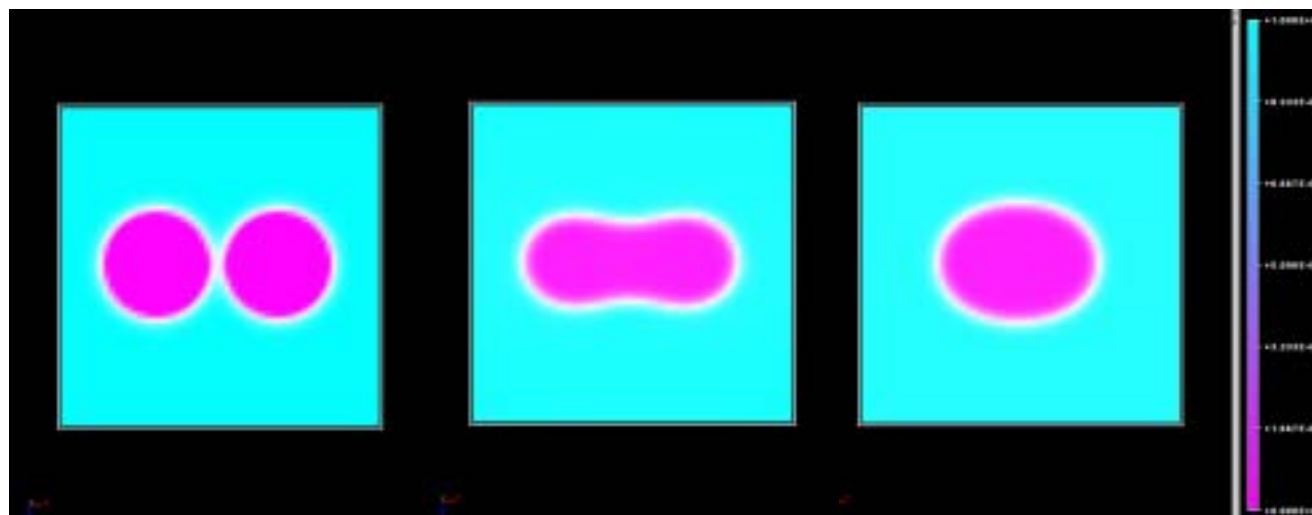
t=1

t=4

t=20

Phase separation
with hydrodynamics
effect.

- Flory-Huggins model.
2-dimensional, Periodic
B.C.

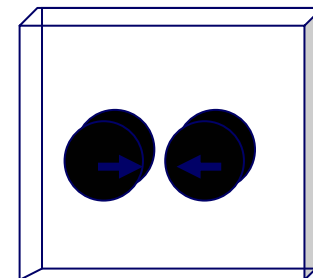


t=0

t=2

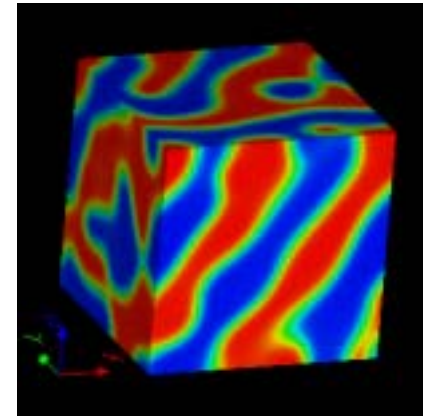
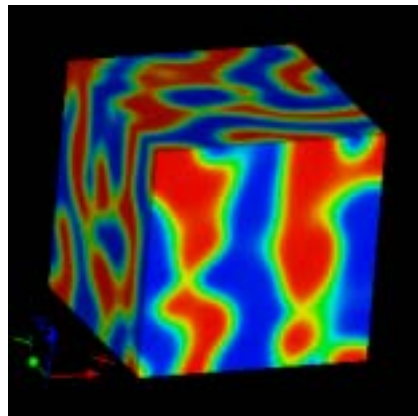
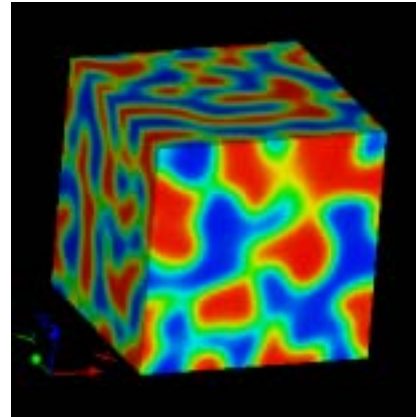
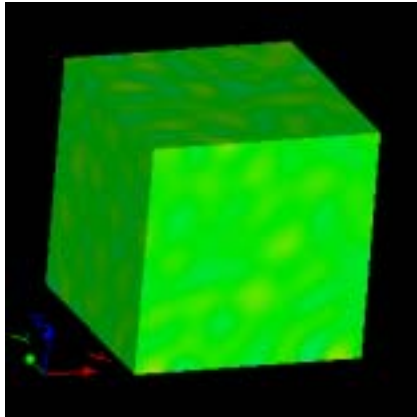
t=10

Coagulation of
2 droplets,
2-dimensional.



Application of “PhaseSeparation FDM”

Phase separation under shear



Simulation of Spin Coating

(An application of “Phase Separation FDM”)

- ◆ Problems for spin coating
 - Surface roughness
 - Phase separated structure inside film

- ◆ Experimental approaches
 - Selectivity to the solvent
 - Adhesion to the substrate
 - Viscosity

- ◆ Proposed models

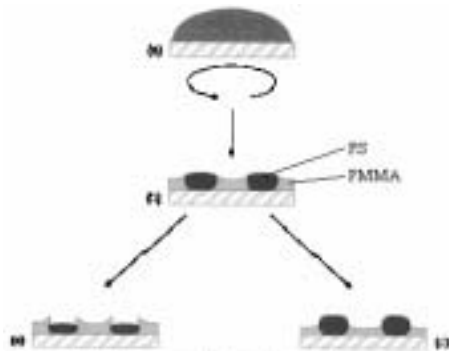


Figure 3. Schematic model describing the formation of the topographic structure during the spin coating process.

Macromolecules, 30, 4995 (1997)

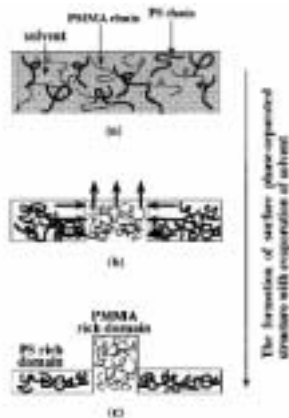


Figure 6. Schematic representation of the formation process of the surface phase-separated structure of the PS/PMMA thin film.

Macromolecules, 29, 3232 (1996)

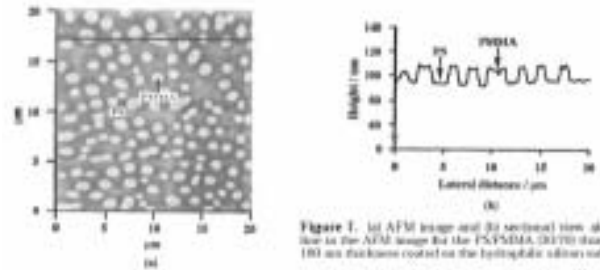


Figure 7. (a) AFM image and (b) vertical view along the line in the AFM image for the PS/PMMA (30/70) thin film of 100 nm thickness coated on the hydrophilic silicon substrate.

Macromolecules, 29, 3232 (1996)

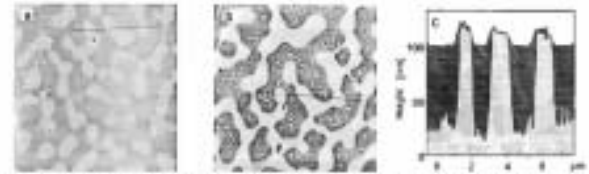


Figure 8. Solvent dependence of the PS/PMMA domain structure spin-coated from THF: (a) on SiO₂; (b) on CGM. The AFM pictures have lateral dimensions of 14 μm × 14 μm. (a, b) as spin-coated; (c) after immersion in chloroform to remove PS; (d) after immersion in acetic acid to remove the PMMA-rich phase. The cross-sections in (a), (b), (d) reveal the vertical distribution of the PS (dark gray) and PMMA (light gray) phases. The error bar in (c) indicates the accuracy of the superposition procedure. PMMA preferentially adheres to the more polar SiO₂ surface to form a homogeneous layer next to the substrate. On the CGM a PS/PMMA bilayer is observed, with PS next to the substrate. The PMMA layer (bright) is punctured by holes that are partially filled by the PS-rich phase (dark).

Macromolecules, 30, 4995 (1997)

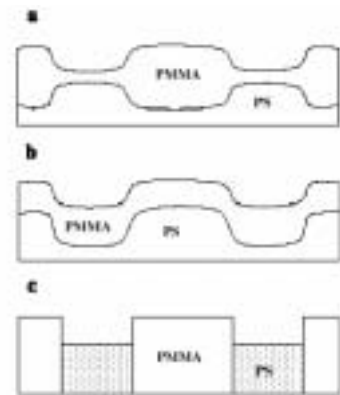


Fig. 8. Structural models of PS/PMMA blends: (a) surface pits correspond to defects in PS-PMMA interface; (b) surface pits correspond to pits in PS-PMMA interface; and (c) complete dewetting of the PS underlayer from model (a). See text for discussion.

Polymer, 42, 1121 (2001)



Spin Coating Simulation

◆ Evaporation of solvent

– evaporation rate

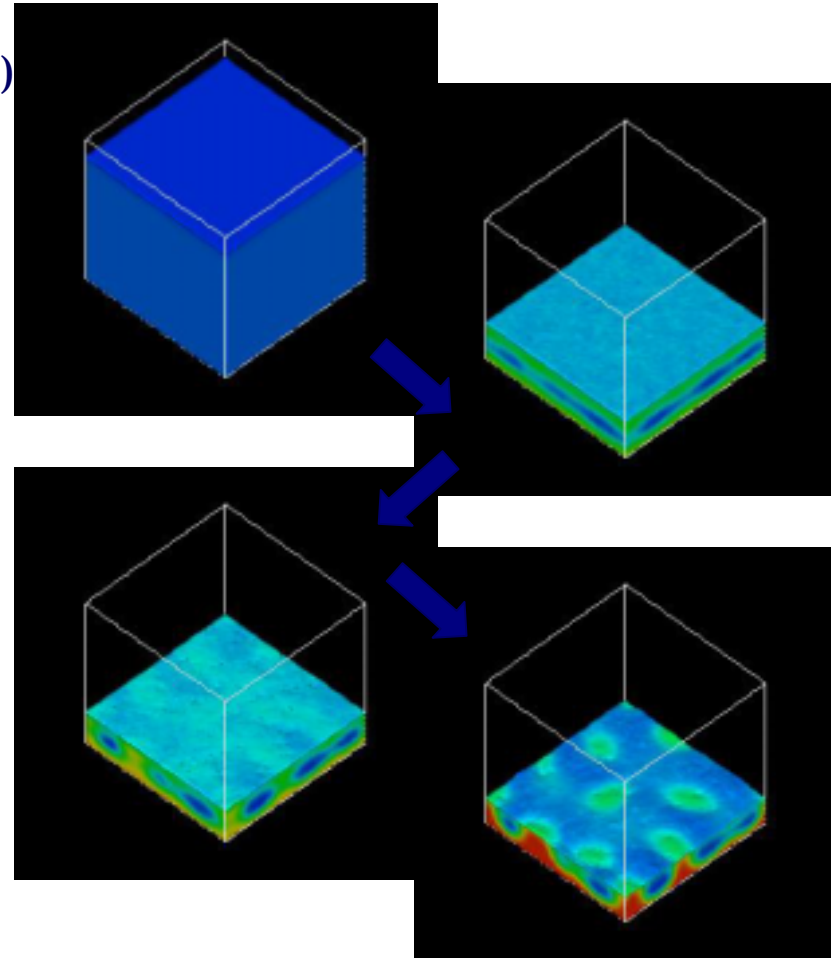
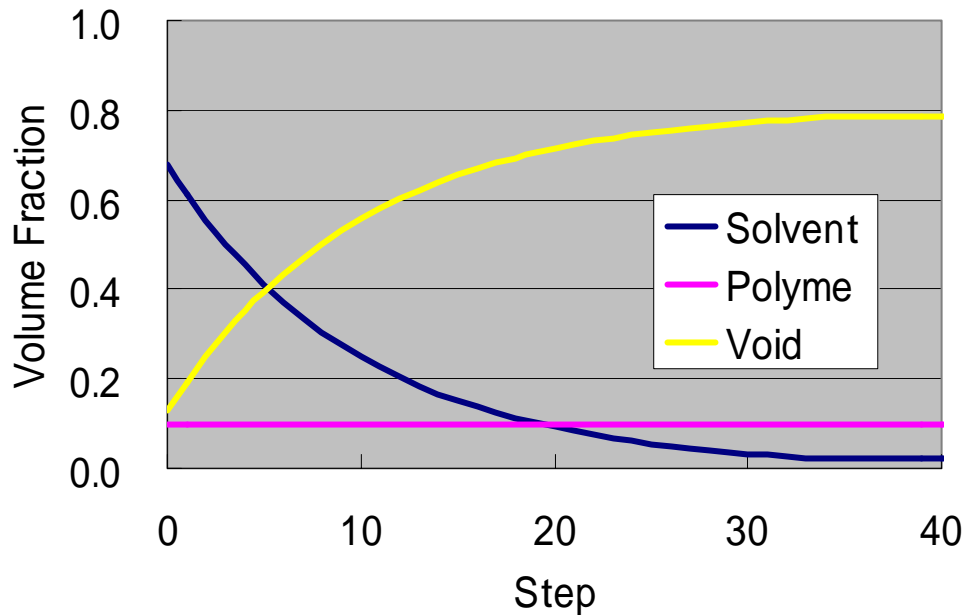
J. Electrochem. Soc., 138, 317 (1991)

$$E = \kappa(x_{I}^0 - x_{I\infty})$$

κ : mass transfer coefficient

x_{I}^0 : initial solv. fraction

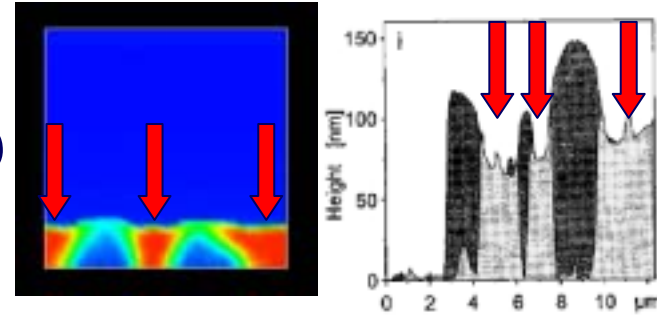
$x_{I\infty}$: equilibrium solv. fraction



Spin Coating Simulation

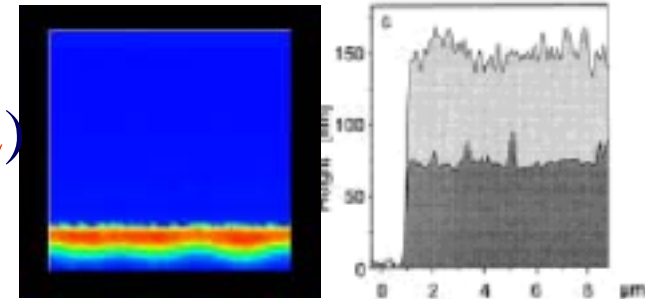
Solvent Selectivity (csolv-poly)

- Poly1 / Poly2 / solvent (better for **Poly1**)
- PMMA / PS / MEK (better for **PMMA**)



Adhesion to the substrate (gS)

- Poly1 / Poly2 /substrate (better for **Poly2**)
- PMMA / PS / ODM (better for **PS**)



Evaporation rate (E)

- related to spinning rate

Viscosity (h)

- effect of hydrodynamic flow

“*Electrolyte*”

Simulate ion kinetics in electrolyte solutions.

3-dimensional FDM and FEM simulators.

Calculate the electro-kinetic phenomena such as electro-osmosis/electro-phoresis etc.)

The equations of Electrolyte

Time evolution of ion density

$$\frac{\partial C_\alpha}{\partial t} = -\nabla \cdot (\mathbf{v} C_\alpha) - \nabla \cdot \mathbf{J}_\alpha.$$

$$\mathbf{J}_\alpha \equiv -L_\alpha \left[k_B T \nabla C_\alpha + e Z_\alpha C_\alpha \nabla \Phi \right].$$

Flow field

$$\mathbf{K} = - \sum_{\alpha=0}^{N_c-1} \left[k_B T \nabla C_\alpha + e Z_\alpha C_\alpha \nabla \Phi \right].$$

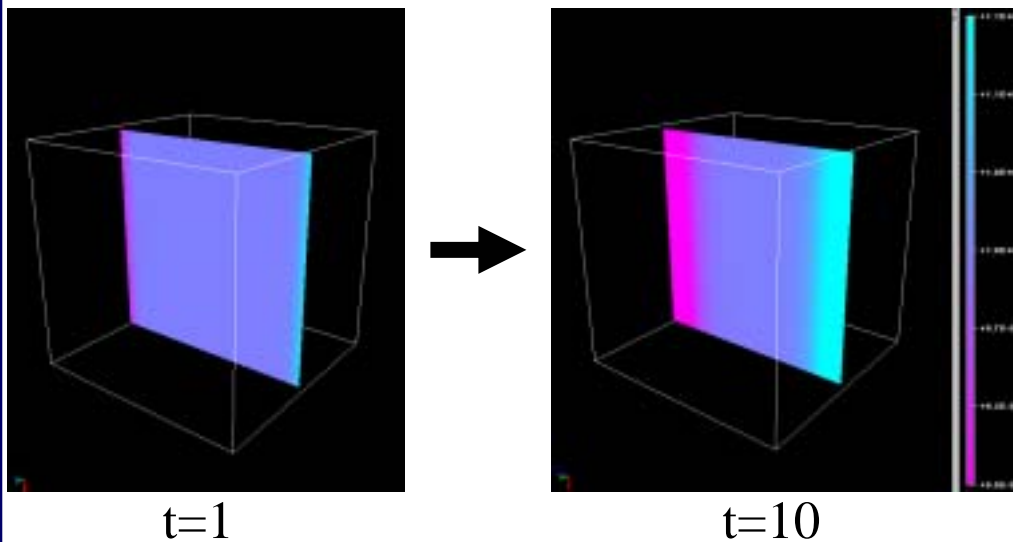
$$-\nabla p + \eta_w \Delta \mathbf{v} + \mathbf{K} = 0$$

Electric field

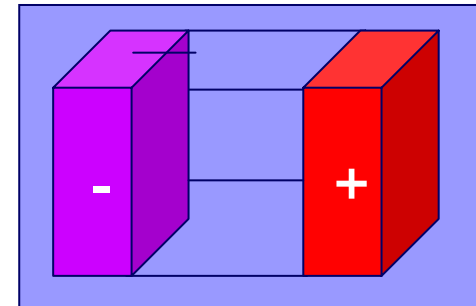
$$\Delta \Phi = -\frac{1}{\epsilon_o \epsilon_r} \sum_{\alpha} e Z_\alpha C_\alpha.$$



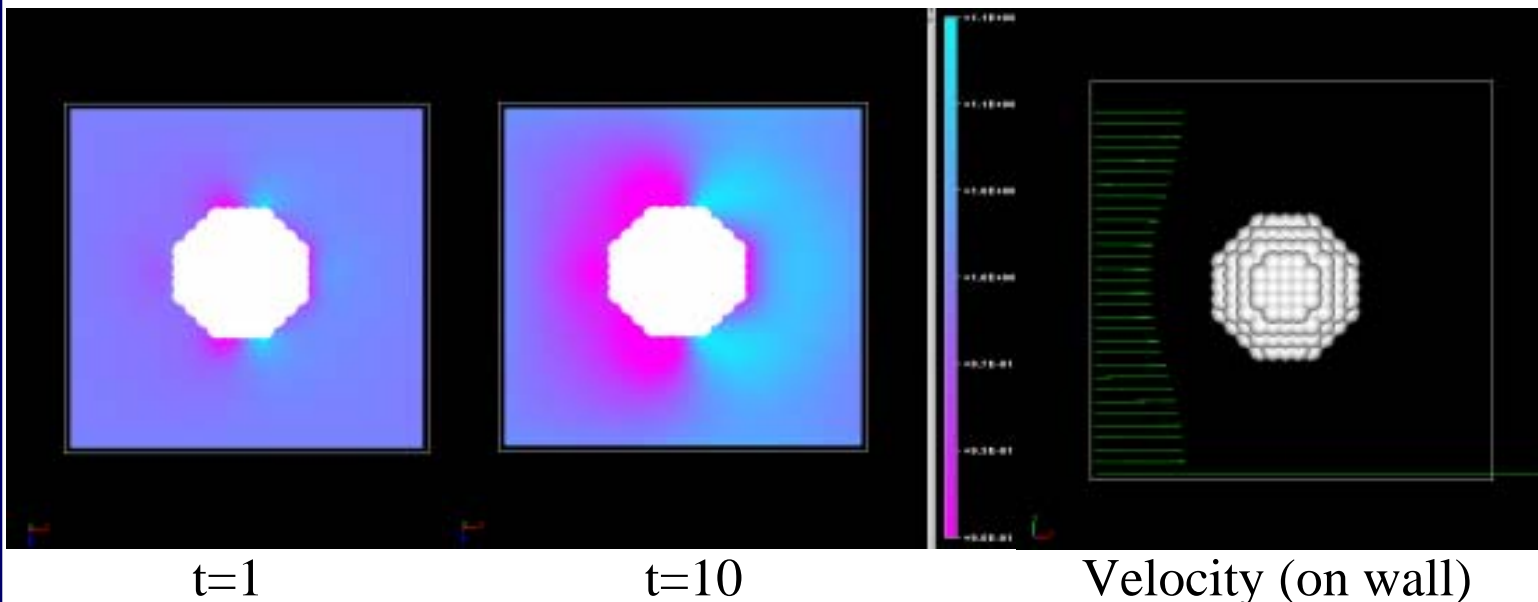
Applications of “Electrolyte FDM”



Ion density distribution

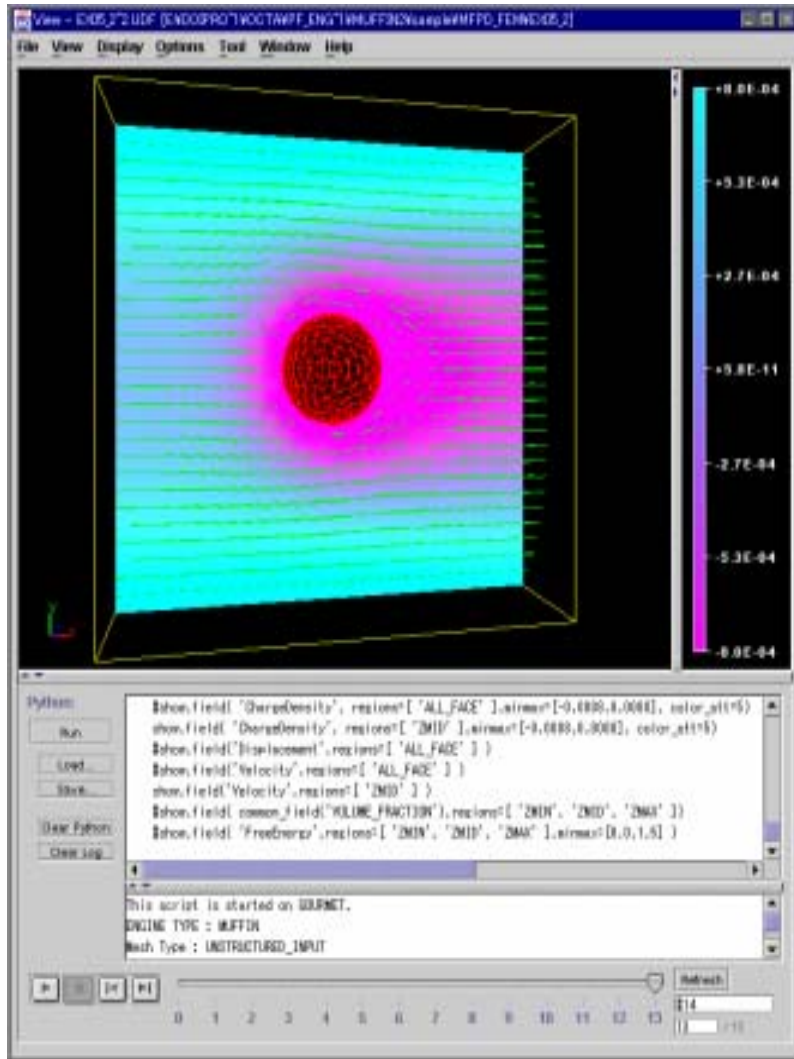


Ion distribution between electrodes under electric field

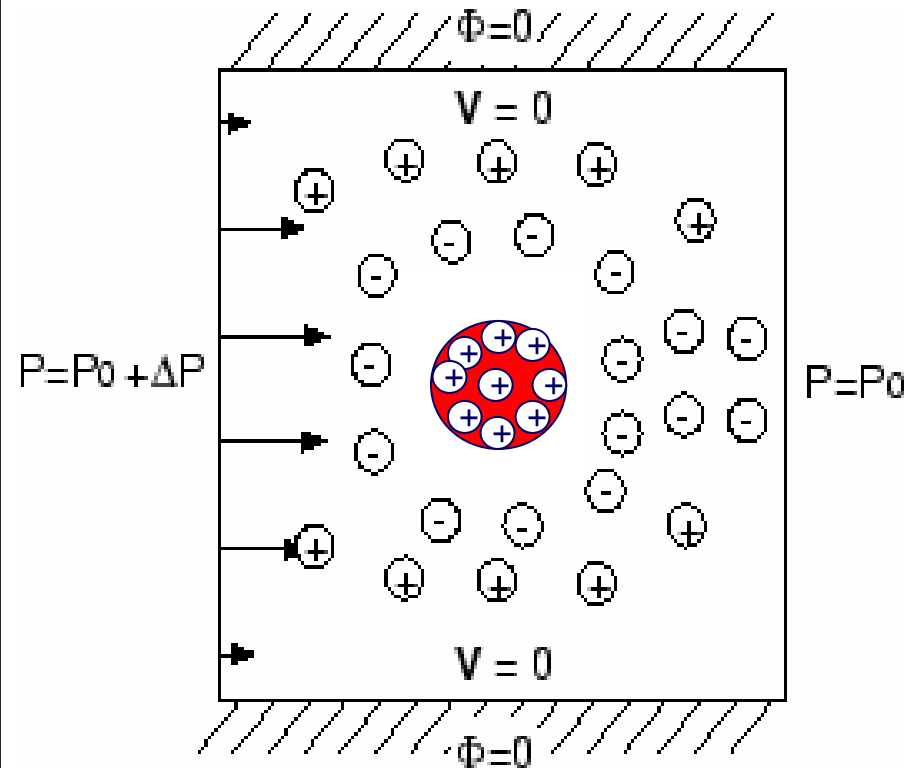


Flow of electrolyte around a charged particle.

Application of “Electrolyte FEM”



Ion distribution around a charged sphere moving in an electrolyte solution

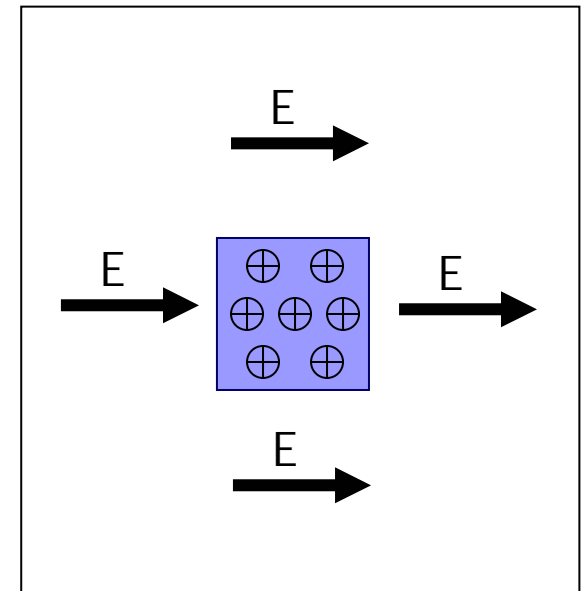
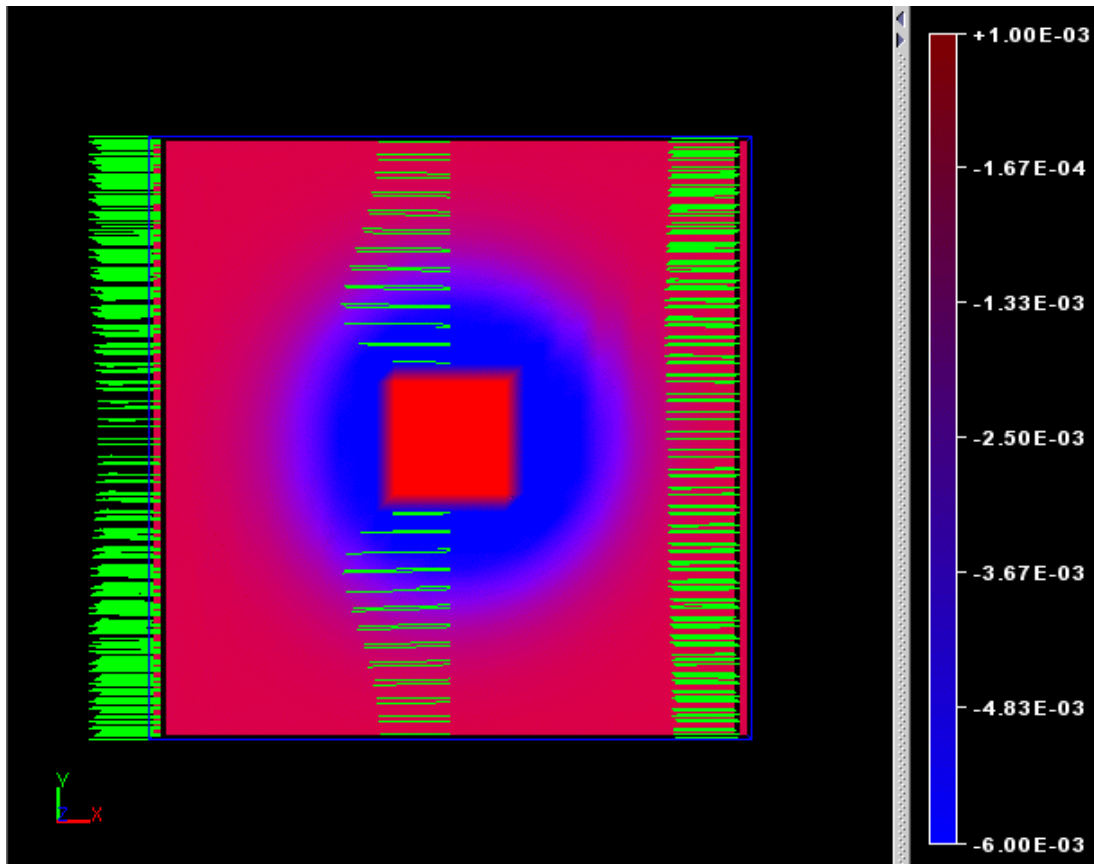


(3-dimensional Delaunay mesh)

Application of “Electrolyte FEM” : Electro osmosis and Electrophoresis

Electrolyte flow induced by electric field around a charged particle

(simulation of electro-osmosis or electro-phoresis)



Micro Fluidics Chip Simulator “*MEMFluid*”

Equations of motion.

Concentration of ions : $\frac{\partial C_\alpha}{\partial t} = -\nabla \cdot (\mathbf{v}C_\alpha) - \nabla \cdot \mathbf{j}_\alpha + \sum_\beta R1_{\alpha\beta} C_\beta + \sum_{\beta,\gamma} R2_{\alpha\beta\gamma} C_\beta C_\gamma$
 (diffusion and reaction)

Flux density of ions : $\mathbf{j}_\alpha = -L_\alpha [k_B T \{ \nabla C_\alpha + \sum_\beta \chi_{\alpha\beta} C_\alpha \nabla C_\beta \} + eZ_\alpha C_\alpha (\nabla\Phi - \mathbf{E}_0)]$

Oseen equation : $0 = -\nabla p + \nabla \left[\eta_w \left\{ \nabla \mathbf{v} + (\nabla \mathbf{v})^t \right\} \right] + \mathbf{K} \quad (\nabla \cdot \mathbf{v} = 0)$
 (laminar flow)

Volume force : $\mathbf{K} = -\sum_\alpha k_B T \{ \nabla C_\alpha + \sum_\beta \chi_{\alpha\beta} C_\alpha \nabla C_\beta \}$ } In Bulk
 Laplace equation : $\nabla^2 \Phi = 0$ } (charge neutrality)

C_α : -ion concentration \mathbf{j}_α : Flux density of -ion L_α : Mobility of -ion

Z_α : Charge of -ion $\chi_{\alpha\beta}$: Interaction parameter between -ion and -ion

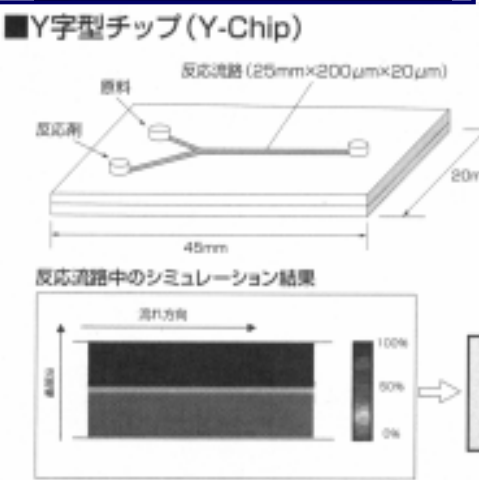
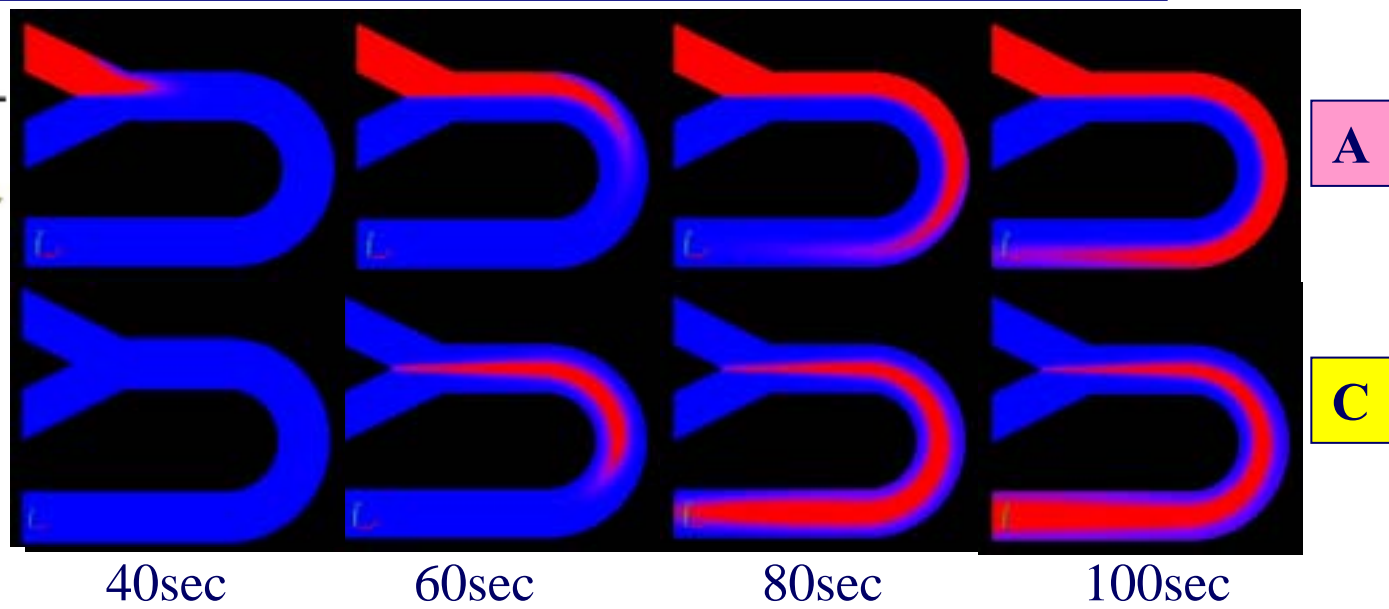
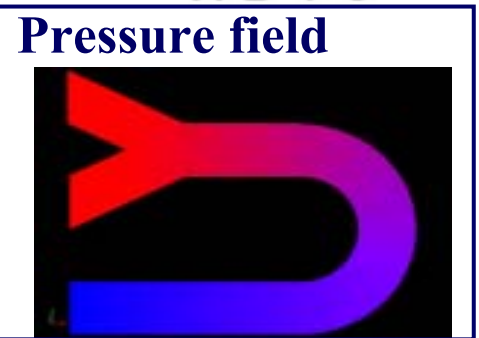
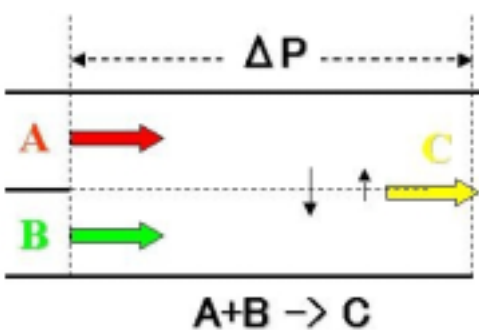
Φ : Electric potential \mathbf{E}_0 : External electric field

Applications.

- ◆ MEMS (Micro Electro Mechanical System), Lab-on-a chip.
- ◆ Micro reactor, μ TAS (Total Analysis System), Bio chips.



Application of “MEMFluid”: Y-shaped micro-reactor



微細流路中では、レイノルズ数が小さいことから流れは層流となる。

原料と反応剤との接触面積が小さいことから合成収率が低いことが予想される。

16cases:

$P=1.0, 2.5, 5.0, 10.0$

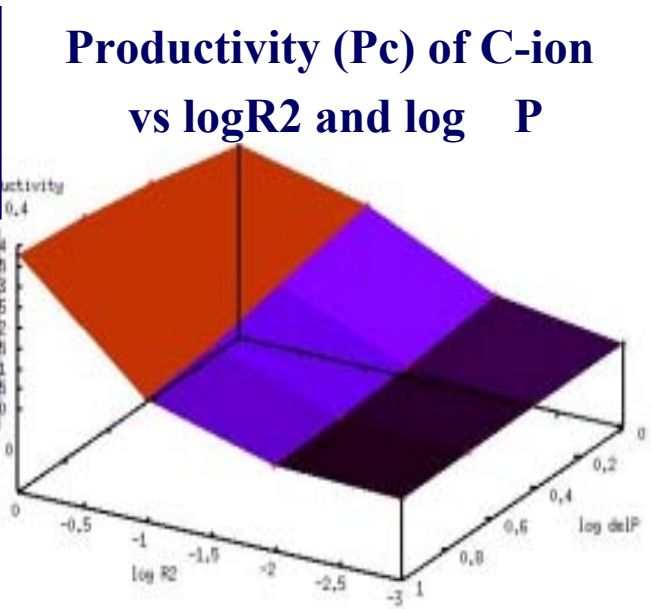
$R2=1e-3, 1e-2, 1e-1, 1.0$

Results:

For increase P_c .

$R2 > 0.4: P \rightarrow 10.0$

$R2 < 0.4: P \rightarrow 1.0$



Application of “MEMFluid” :Electro-osmotic chip

Velocity on boundary is determined by electro-kinetics

- ◆ Velocity at the boundary :

$$\mathbf{v}_{eo} = \frac{\varepsilon}{\eta_w} \zeta \mathbf{E}$$

Helmholtz-Smoluchowski eq.

- ◆ Calculation of ζ -potential on boundary:

- 1-dim Poisson-Boltzmann eq. (1-1 electrolyte)

$$\zeta = \frac{2k_B T}{Ze} \ln \left[\frac{\sigma}{(8C\varepsilon k_B T)^{1/2}} + \left(\frac{\sigma^2}{8C\varepsilon k_B T} + 1 \right)^{1/2} \right]$$

Simulation result:

P=10.0, R2=1.0

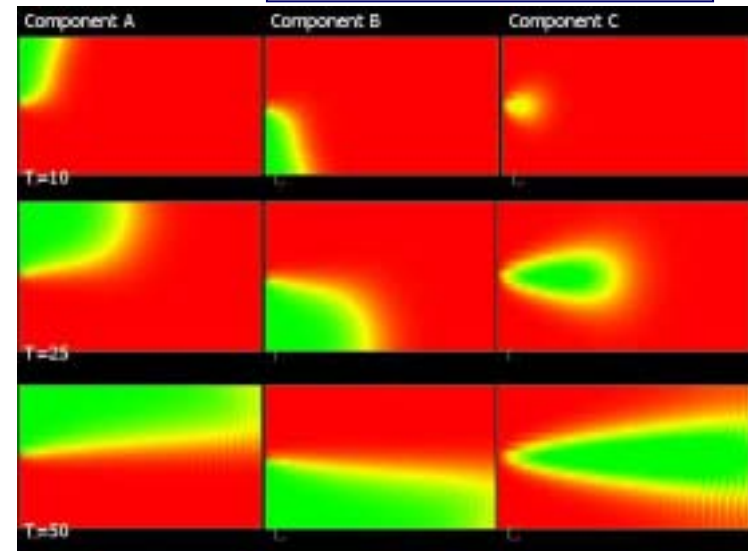
- Condenser model (linear approximation)

valid for $Ze|\zeta|/k_B T \ll 1$ $\zeta \leq 25(mV)$

$$\left\{ \begin{array}{l} \zeta = \frac{\sigma}{\varepsilon \kappa} \\ \kappa = \left(\frac{\sum Z_\alpha^2 C_\alpha e^2}{\varepsilon k_B T} \right)^{1/2} \end{array} \right.$$

Scaling factor: Debye length/System size :

$$\frac{l_b}{l} = \frac{e^2}{(k_B T \varepsilon l)} \approx 10^{-3} - 10^{-2}$$



“*Elastica*”

Basic model: linear elasticity, 3-dimensional FEM

$$F\{u_i(\mathbf{x})\} = \int_V d^d x \{f\} - \int_V d^d x \rho(\mathbf{x}) g_i u_i(\mathbf{x}) - \int_{S_t} d^{d-1} x T_i u_i(\mathbf{x})$$

isotropic elastic material

$$f = G(\mathbf{x}) \left(e_{ij} - \frac{1}{d} \delta_{ij} e_{ll} \right)^2 + \frac{K(\mathbf{x})}{2} (e_{ll})^2$$

$$e_{ij} = \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$$

anisotropic elastic material (axissymmetric)

$$f = D_1 (e_{ii})^2 + D_2 (n_i n_j e_{ij})^2 + D_3 (e_{ll} \cdot n_i n_j e_{ij}) + D_4 n_l e_{il} \cdot n_k e_{ik} + D_5 e_{ij} e_{ij}$$

Arbitrary mixture and morphology of isotropic/anisotropic materials.

Stiffness Matrix for Anisotropic elasticity (axissymmetric)

$$\begin{bmatrix} \sigma_{xx} \\ \sigma_{yy} \\ \sigma_{zz} \\ \sigma_{yz} \\ \sigma_{zx} \\ \sigma_{xy} \end{bmatrix} = \begin{bmatrix} n & l & l & 0 & 0 & 0 \\ l & k+m & k-m & 0 & 0 & 0 \\ l & k-m & k+m & 0 & 0 & 0 \\ 0 & 0 & 0 & m & 0 & 0 \\ 0 & 0 & 0 & 0 & \mu & 0 \\ 0 & 0 & 0 & 0 & 0 & \mu \end{bmatrix} \begin{bmatrix} e_{xx} \\ e_{yy} \\ e_{zz} \\ e_{yz} \\ e_{zx} \\ e_{xy} \end{bmatrix}$$

$$f = D_1 (e_{ii})^2 + D_2 (n_i n_j e_{ij})^2 + D_3 (e_{ll} \cdot n_i n_j e_{ij}) + D_4 n_l e_{il} \cdot n_k e_{ik} + D_5 e_{ij} e_{ij}$$

$$\begin{cases} D_1 = (k-m)/2 \\ D_2 = (n+k-m)/2 - l - \mu \\ D_3 = l - k + m \\ D_4 = \mu - m \\ D_5 = m \end{cases}$$

Application of “Elastica” : Elasticity of the two phase structure calculated by SUSHI.

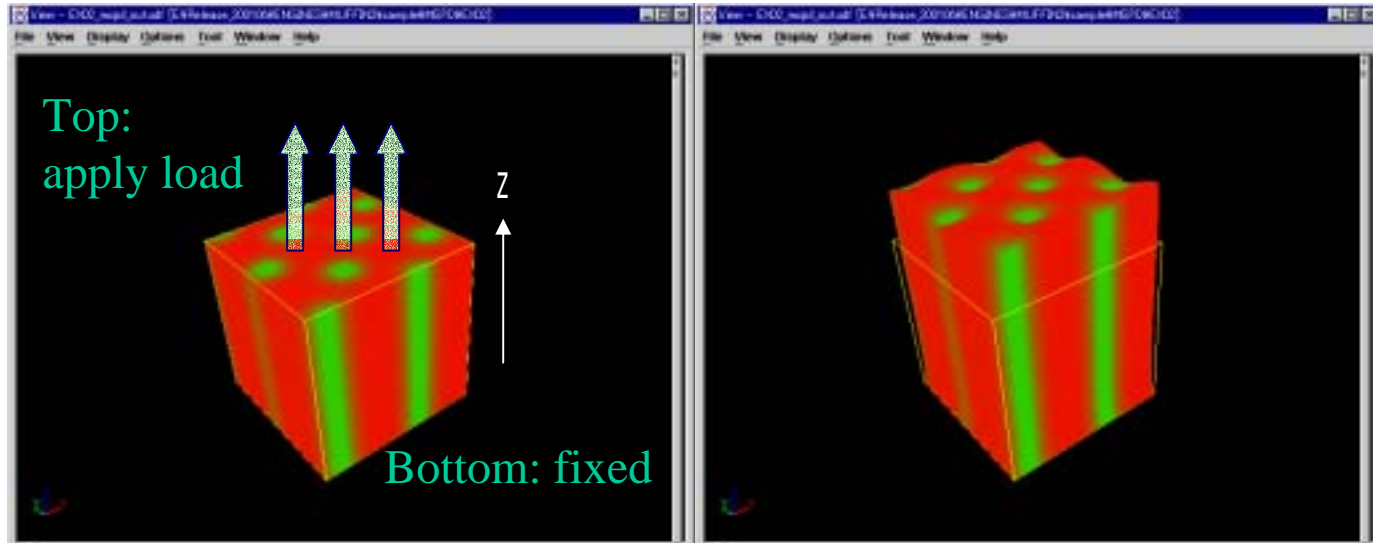
T.Yamaue
M.Sasaki

【Before deformation】

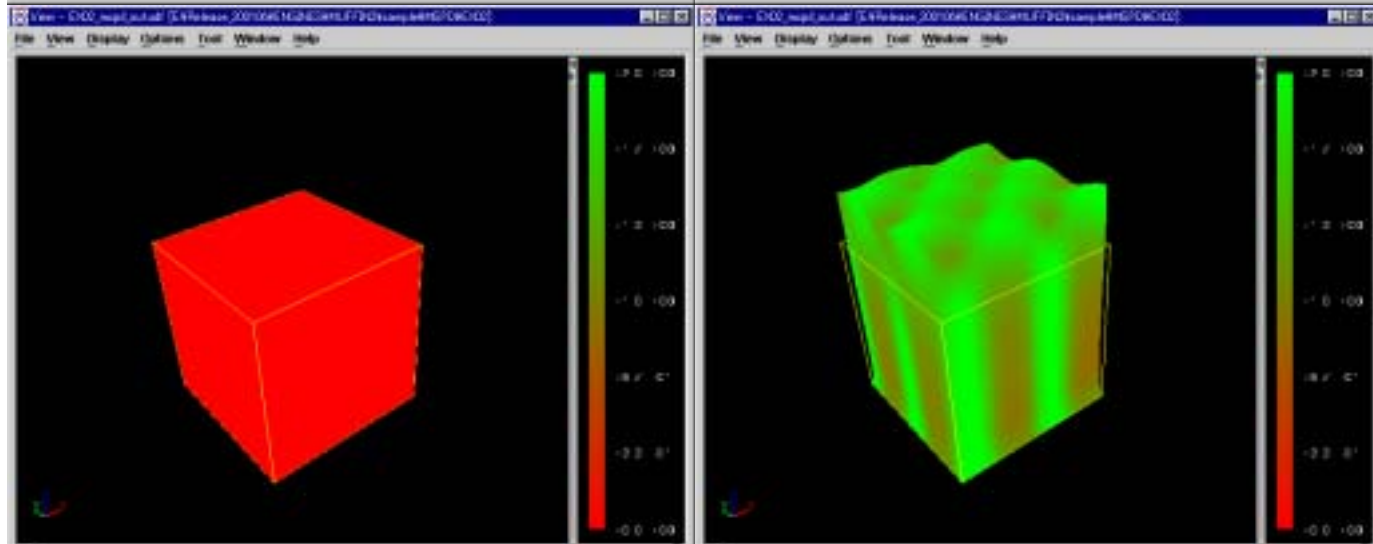
【after deformation】

【Volume fraction】

- component1 (green)
z : hard, x, y : soft
- component2 (red)
x, y : hard, z : soft

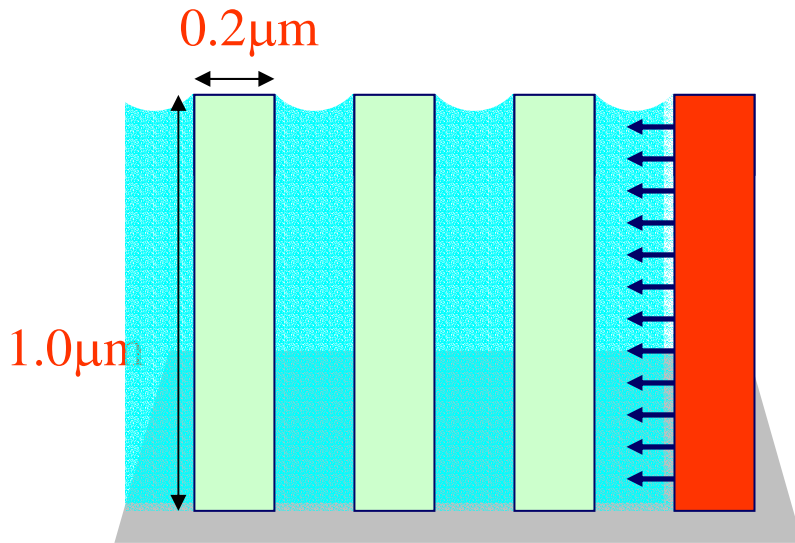


【Strain energy】



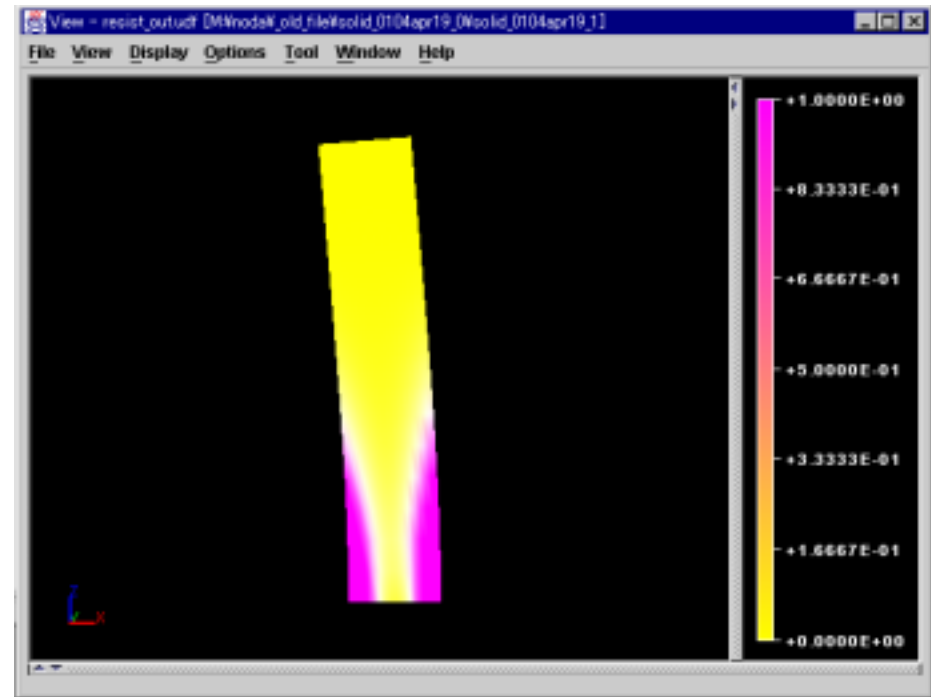
Application of “Elastica”: Deformation of photo regist pattern by capillary force

M.Noda
M.Sasaki

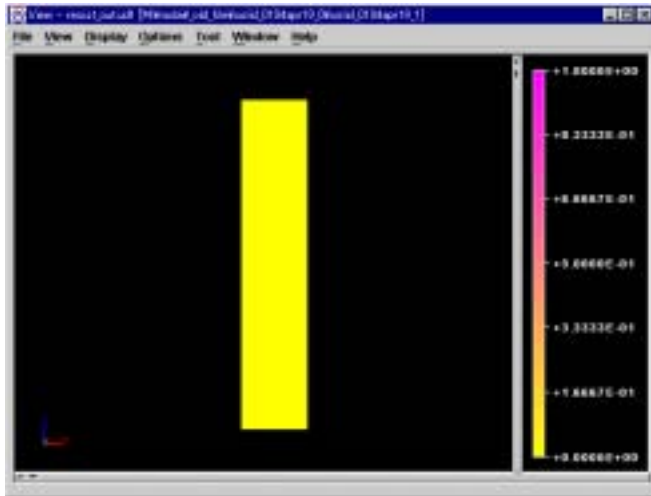


negative pressure induced by the capillary force

[after deformation] Strain energy



[before deformation]



Application of “Elastica”: Effective modulus of two phase system for various morphology

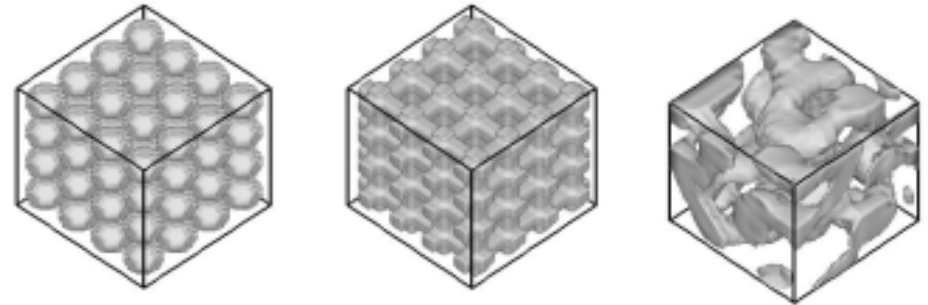
Total free energy and effective modulus

$$F = \bar{G} \sum \left\{ \left(e_{ij} - \frac{1}{d} \delta_{ij} e_{ll} \right)^2 \right\} + \bar{K} \sum \left(\frac{1}{2} e_{kk}^2 \right)$$

Effective modulus is calculated by independent deformation modes

$$\bar{K} = - \frac{\sum \left\{ \left(e_{ij} - \frac{1}{d} \delta_{ij} e_{ll} \right)^2 \right\}}{\sum \left(\frac{1}{2} e_{kk}^2 \right)} \bar{G} + \frac{F}{\sum \left(\frac{1}{2} e_{kk}^2 \right)}$$

Morphology (PP + Elastomer)



(a)dispersed (b)bi-continuous (C) by SUSHI

Calculated Young’s modulus

modulus	\bar{E}	analytic-model
sphere	3.753	series
bi-continuous	34.67	Davies
sushi1	91.84	
sushi2	50.99	

sushi2: volume fraction is reset to 0 and 1 using a threshold value.

“GelDyna”

Equations of motion. (Stress-Diffusion Coupling Model for Gels)

$$\text{Velocity of polymer : } \zeta (\mathbf{v}_p - \mathbf{v}_s) = - \phi \nabla \cdot p + \nabla \cdot \underline{\underline{\boldsymbol{\sigma}}}$$

$$\text{Velocity of solvent : } \zeta (\mathbf{v}_s - \mathbf{v}_p) = - (1 - \phi) \nabla \cdot p$$

$$\text{incompressibility : } \nabla \cdot [\phi \mathbf{v}_p + (1 - \phi) \mathbf{v}_s] = 0$$

\mathbf{V}_p : velocity of polymer

\mathbf{V}_s : velocity of solvent

ϕ : volume fraction of polymer

p : pressure

ζ : friction coefficient

$\underline{\underline{\boldsymbol{\sigma}}}$: Cauchy stress tensor of polymer

Free energy of Gels.

$$F = \frac{k_B T}{v_1} \int d^d x [(1 - \phi) \ln(1 - \phi) + \chi \phi (1 - \phi) + \frac{1}{2} v_0 \frac{\phi}{\phi_0} (tr \underline{\underline{\mathbf{W}}} + 2 \ln \frac{\phi}{\phi_0})]$$

Stress of polymer networks

$$\sigma_{ij} = - [\phi f_m'(\phi) - f_m(\phi)] \delta_{ij} + v_0 \frac{\phi}{\phi_0} (W_{ij} - \delta_{ij})$$

$$\text{mixing free energy (Flory-Huggins): } f_m(\phi) = (1 - \phi) \ln(1 - \phi) + \chi \phi (1 - \phi)$$

W_{ij} : finger strain tensor

ϕ_0 : volume fraction of polymer in the relaxed state

χ : polymer-solvent interaction

v_0 : crosslink number density in the relaxed state

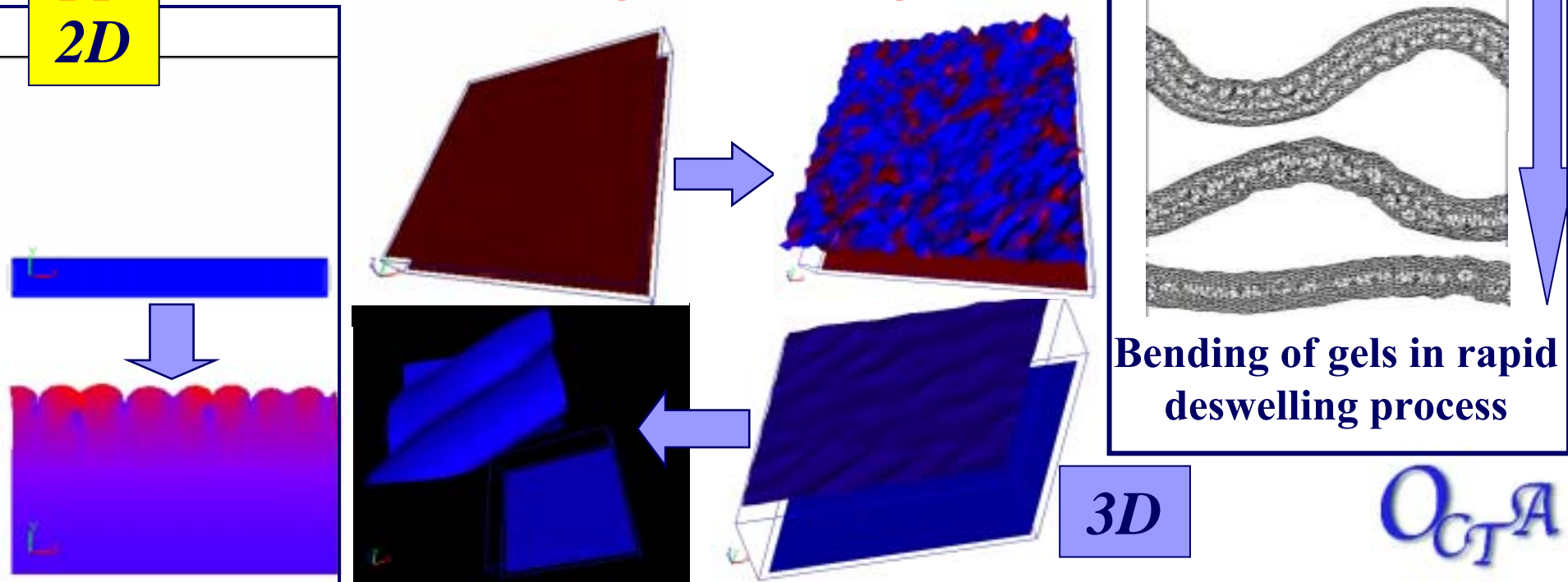


Applications of “GelDyna”

Applications.

- ◆ Super-water absorbing gels
- ◆ Temperature sensitive gels.
- ◆ Drug delivery systems (DDS)
- ◆ Actuators, sensors and switching devices.

Applications to swelling of NIPA gels.



Light Transmittance Simulator

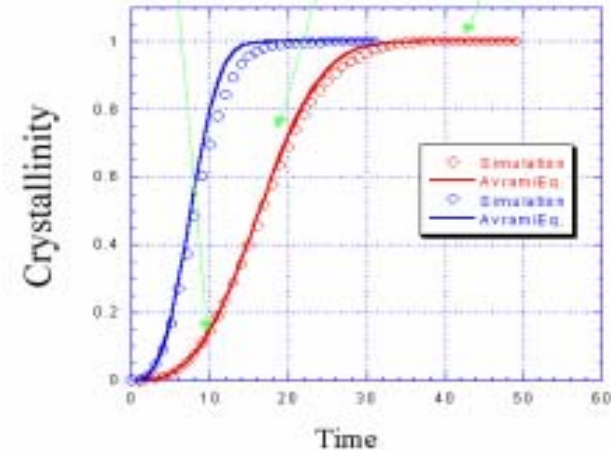
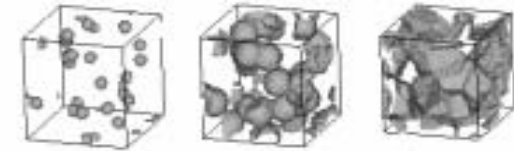
“TURBAN”

=TURBidity ANalyzer

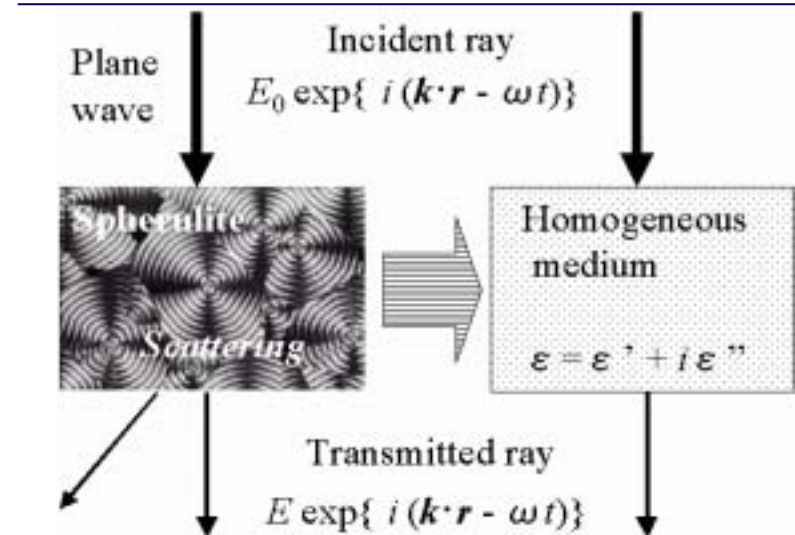
“TURBAN” predicts the transparency of polymeric material having spherulite structures.

“TURBAN” consists of two parts:

- (i) Calculate the spherulite growth based on Avrami models.
- (ii) Calculate the light transmittance based on Maxwell equation.



The image of the spherulite growth simulator.



The model figure about the light which penetrates spherulite system.

“TURBAN” sample work

Light transmittance prediction of a PE film

Simulation conditions:

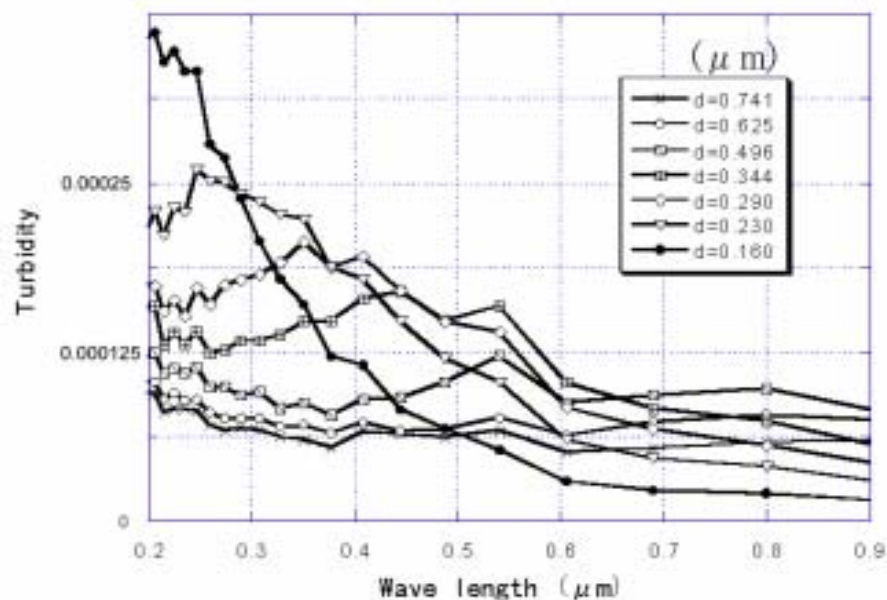
- in the cubic cell of 128^3
- a visible light wavelength = 400-700nm
- non-uniform nucleation
- using known properties of PE blown film

Result:

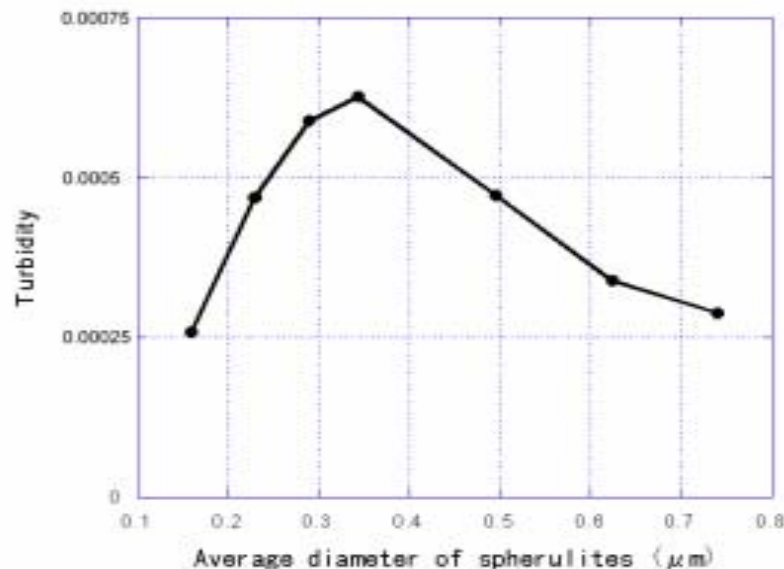
The peak of turbidity is seen near the wavelength comparable to the mean spherulite diameter.

The peak of the turbidity is in the lower range of a visible light.

These calculation are in good agreement with experiments.



The turbidity spectra for system with the various average spherulite diameters.



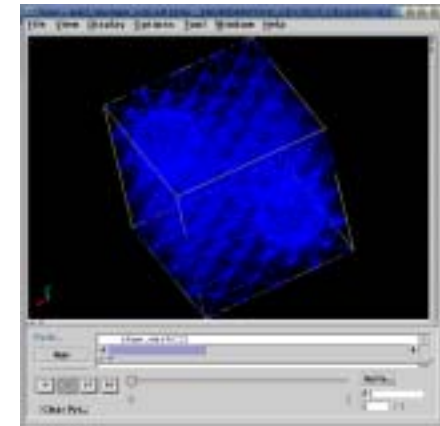
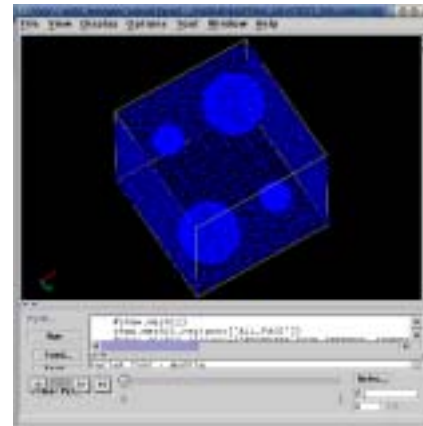
The turbidity integration value for the visible light in each spherulite diameter.

Support tools of MUFFIN

T.Yamaue
A.Kuroda

”Pre-processors”

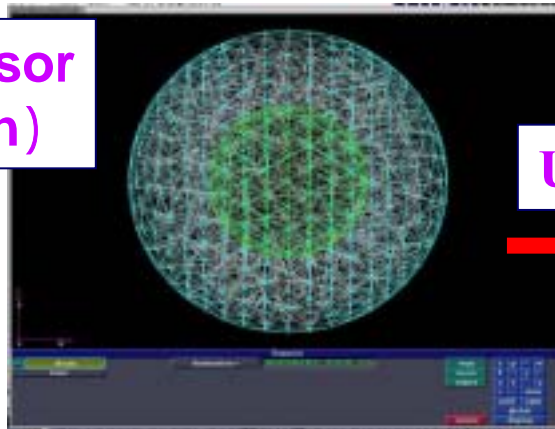
- ◆ “**MILK**” (Mesh Generator)
 - Delaunay3D/2D auto meshing.
 - Tetrahedron and Triangle.
 - Internal Structures.



- ◆ “**NASTRAN BULK FILTER**”

- Import NASTRAN BULK mesh data to UDF mesh data.

FEM pre-processor
(ex. HyperMesh)



UDF convert



GOURMET



- ◆ “**MeshFieldConvertor (IMPORT/EXPORT_...)**”

- Import/Export fields (morphology) data with SUSHI.

OCTA

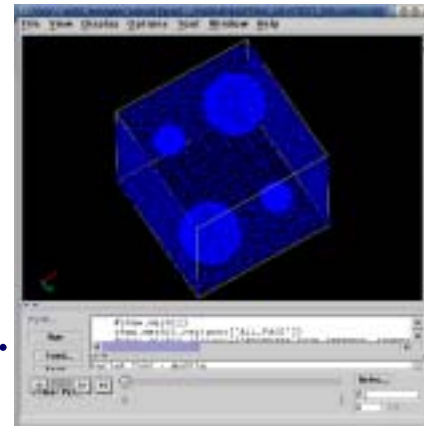
Support tools of MUFFIN

T.Yamaue
T.Taniguchi
M.Sasaki

”Post-processors”

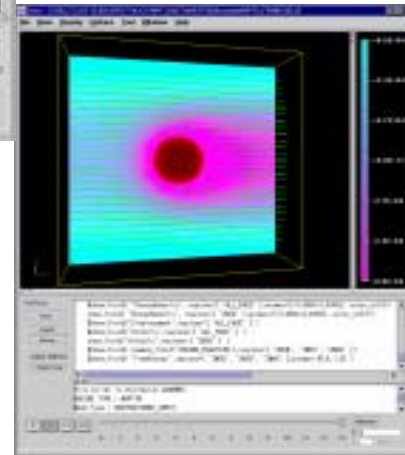
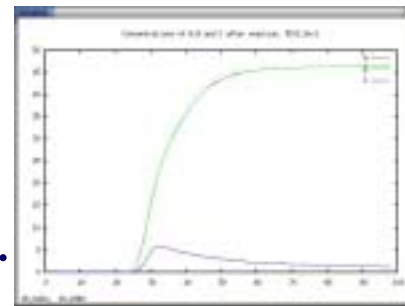
◆ “MeshFieldShow (SHOW_...)”

- Show mesh and field.
- Structured and Unstructured.
- Any cross section and Partial Regions.



◆ “MeshFieldPlot (PLOT_...)”

- Plot field (using gnuplot).
- Structured and Unstructured.
- Any cross section and Partial Regions.

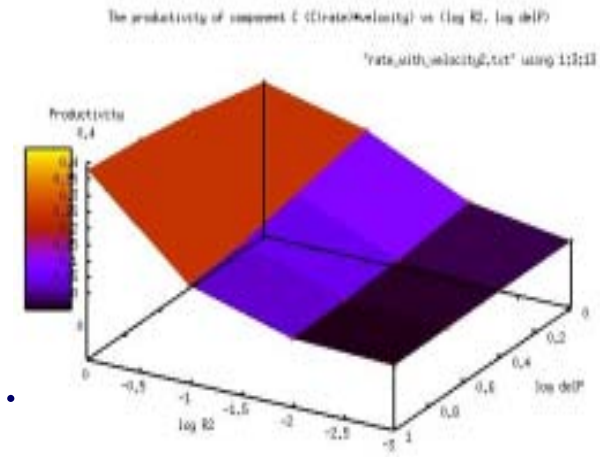


◆ “udf2avs”

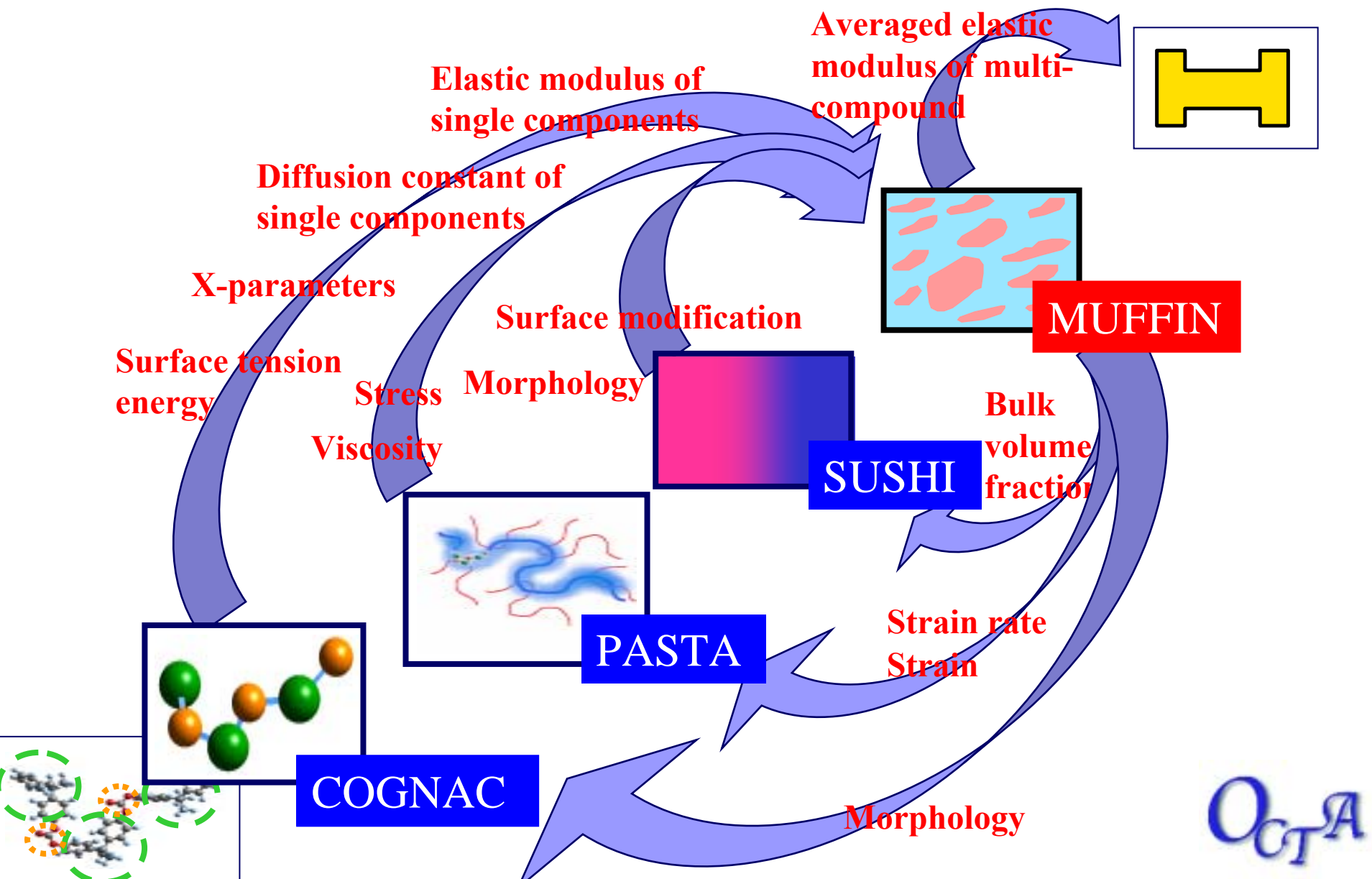
- Convert UDF field to AVS field.
- Structured and Unstructured.

◆ Some Support tools for each package.

- “ModelingSupporter”, “analyze_reactor”,



MUFFIN : Linking to other layers



Summary

- ◆ MUFFIN (MultiFarious Field simulator for Non-equilibrium system) is an architecture for simulations of spatio-temporal behavior of multi-phase polymeric systems ($\sim 0.1 \mu\text{m}$ to 1mm , $\sim \text{sec}$).
- ◆ Six simulation engines, “**PhaseSeparation**”, “**Electrolyte**”, “**MEMFluid**”, “**Elastica**”, “**GelDyna**” and “**TURBAN**” are implemented.
- ◆ MUFFIN is designed by the object-oriented modeling and serves various reusable components libraries, such as structured and unstructured mesh, foundation of fields, I/O routines, matrix solvers, finite elements solvers and “**DynamicsManager**”.
- ◆ The MUFFIN component library will be useful for you to construct your own simulator.